

# Three-Factor ANOVA

PSYC214: Statistics For Group Comparisons

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Week 9

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Three-Factor  
ANOVA

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Context

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## Learning Objectives

- Procedures for analysing and interpreting three-factor ANOVA
- How to decompose a three-way interaction:
  - splitting the design and analysing it as a series of two-factor ANOVAs
- Examples:
  - $2 \times 2 \times 2$  fully within-participants ANOVA
  - $2 \times 2 \times 2$  mixed ANOVA
- General things to consider

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## Three-Factor ANOVA

- Three-factor ANOVAs are common in psychology
- In such designs, there are three possible **two-way interactions**:
  - $A \times B$
  - $A \times C$
  - $B \times C$
- There is also the possibility of a **three-way interaction**:
  - $A \times B \times C$
- Complexity of interpreting these designs arises when the three-way interaction is significant

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## Three-Factor ANOVA

- Basic design principles of earlier lectures still apply
- A between-participants design is still relatively simple, with only a single error term for all effects
- However, a  $2 \times 2 \times 2$  design would require at least 160 participants (obeying our maxim of  $N = 20$  per cell)
- Problems with fully within-participants and mixed designs apply equally to three-factor designs
- Try to avoid exceeding two levels per factor where possible

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## Three-Factor ANOVA

- The most straightforward outcome is when the three-way interaction is not significant
- Where this occurs, one or more of the two-way interactions may be significant
- In which case, each significant two-way interaction should be investigated separately of the others
- The procedures for interpreting each interaction are the same as those discussed in previous lectures
- For example, if the  $A \times B$  two-way interaction is significant, the simple main effects of factor A at B, and factor B at A can be investigated

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## Three-Factor ANOVA

- The simplest case arises when none of the interactions are significant
- In this case, the outcome must be interpreted in terms of the main effects, if any of these are significant
- If nothing is significant, then unless specific pairwise comparisons are planned, the analysis is complete

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## Dealing With A Significant Three-Way Interaction

- A significant three-way interaction occurs when there are different two-way interactions between two of the factors according to the levels of the third factor
- The simplest way to analyse a significant three-way interaction is to reanalyse it as a series of two-factor ANOVAs, e.g. :
  - 1 a 2 (factor A: level  $A_1$  vs. level  $A_2$ )  $\times$  2 (factor B: level  $B_1$  vs. level  $B_2$ ) ANOVA at level  $C_1$  of factor C
  - 2 a 2 (factor A: level  $A_1$  vs. level  $A_2$ )  $\times$  2 (factor B: level  $B_1$  vs. level  $B_2$ ) ANOVA at level  $C_2$  of factor C
- Any significant interactions would be followed up with a simple main effects analysis

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## Memory and Context: A 2 $\times$ 2 $\times$ 2 Fully Within-Participants Design

- A memory researcher wants to know if memory is better when material is tested in the same context it was learned in
- They also want to know whether recall and recognition memory are equally context dependent
- The researcher manipulates three factors in a  $2 \times 2 \times 2$  fully within-participants design:
  - 1 memory test (recall vs. recognition)
  - 2 learning context (learn under water vs. learn land)
  - 3 testing context (test under water vs. test land)
- Participants given words to remember in a learning context  $\rightarrow$  memory for the words tested via recall or recognition
- Dependent measure is the number of words remembered correctly

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## Raw Data For Memory and Context Study

Table:  $A \times 2 \times 2$  factorial design

Factor A: Task	Level A <sub>1</sub> recall				Level A <sub>2</sub> recognition			
	Level B <sub>1</sub> under		Level B <sub>2</sub> land		Level B <sub>1</sub> under		Level B <sub>2</sub> land	
Factor C: Testing	C <sub>1</sub> under	C <sub>2</sub> land	C <sub>1</sub> under	C <sub>2</sub> land	C <sub>1</sub> under	C <sub>2</sub> land	C <sub>1</sub> under	C <sub>2</sub> land
P <sub>1</sub>	8	5	3	7	5	5	7	6
P <sub>2</sub>	9	6	3	8	7	6	5	8
P <sub>3</sub>	7	5	4	6	6	7	5	6
P <sub>4</sub>	8	4	4	5	7	5	6	5
P <sub>5</sub>	6	3	3	8	5	4	6	4

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## Aggregate Data For Memory and Context Study

Table:  $A \times 2 \times 2$  factorial design

	Level A <sub>1</sub> recall task			Level A <sub>2</sub> recognition task		
	Level B <sub>1</sub> under	Level B <sub>2</sub> land	Overall	Level B <sub>1</sub> under	Level B <sub>2</sub> land	Overall
Level C <sub>1</sub> under water	7.6	3.4	5.5	6	5.8	5.9
Level C <sub>2</sub> on land	4.6	6.8	5.7	5.4	5.8	5.6
Overall	6.1	5.1	5.6	5.7	5.8	5.8

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## ANOVA Table For Memory and Context Study

Source	Sum of Squares	Degrees of Freedom	Mean Square	F	P
A (memory task)	0.225	1	0.225	1.000	0.374
Error A × P	0.900	4	0.225		
B (learning context)	2.025	1	2.025	1.588	0.276
Error B × P	5.100	4	1.275		
C (testing context)	0.025	1	0.025	0.014	0.911
Error C × P	7.100	4	1.775		
A × B	3.025	1	3.025	2.951	0.161
Error A × B × P	4.100	4	1.025		
A × C	0.625	1	0.625	0.714	0.446
Error A × C × P	3.500	4	0.875		
B × C	30.625	1	30.625	27.222	0.006
Error B × C × P	4.500	4	1.125		
A × B × C	21.025	1	21.025	27.129	0.006
Error A × B × C × P	3.10	4	0.775		
P (participants)	10.900	4	2.733		

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Error B × P	5.100	4	1.275		
C (testing context)	0.025	1	0.025	0.014	0.911
Error C × P	7.100	4	1.775		
A × B	3.025	1	3.025	2.951	0.161
Error A × B × P	4.100	4	1.025		
A × C	0.625	1	0.625	0.714	0.446
Error A × C × P	3.500	4	0.875		
B × C	30.625	1	30.625	27.222	0.006
Error B × C × P	4.500	4	1.125		
A × B × C	21.025	1	21.025	27.129	0.006
Error A × B × C × P	3.10	4	0.775		
P (participants)	10.900	4	2.733		

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## Interpreting The Significant Three-Way Interaction

- To decompose our significant three-way interaction, we first need to decide which factor to split our design by
- The obvious choice is factor A (memory task: recall vs. recognition)
- Next, we perform two two-factor ANOVAs:
  - 2 (learning context: learn under water vs. learn land)  $\times$  2 (testing context: test under water vs. test land) ANOVA for the **recall** memory test condition only
  - 2 (learning context: learn under water vs. learn land)  $\times$  2 (testing context: test under water vs. test land) ANOVA for the **recognition** memory test condition only

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## ANOVA Table For Recall Memory Task

Source	Sum of Squares	Degrees of Freedom	Mean Square	F	P
B (learning context)	5.000	1	5.000	3.636	0.129
Error B $\times$ P	5.500	4	1.375		
C (testing context)	0.200	1	0.200	0.186	0.688
Error C $\times$ P	4.300	4	1.075		
B $\times$ C	51.200	1	51.200	62.061	0.001
Error B $\times$ C $\times$ P	3.300	4	0.825		
P (participants)	5.300	4	1.333		

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## ANOVA Table For Recall Memory Task

Source	Sum of Squares	Degrees of Freedom	Mean Square	F	P
B (learning context)	5.000	1	5.000	3.636	0.129
Error B $\times$ P	5.500	4	1.375		
C (testing context)	0.200	1	0.200	0.186	0.688
Error C $\times$ P	4.300	4	1.075		
B $\times$ C	51.200	1	51.200	62.061	0.001
Error B $\times$ C $\times$ P	3.300	4	0.825		
P (participants)	5.300	4	1.333		

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## Simple Main Effects Table For Recall Memory Task

Source	Sum of Squares	Degrees of Freedom	Mean Square	F	P
learning context at					
test under water	44.100	1	44.100	32.073	0.005
test land	12.100	1	12.100	8.800	0.041
Error term	5.50	4	1.375		
testing context at					
learn under water	22.500	1	22.500	20.930	0.010
learn land	28.900	1	28.900	26.884	0.007
Error term	4.300	4	1.075		

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## ANOVA Table For Recognition Memory Task

Source	Sum of Squares	Degrees of Freedom	Mean Square	F	P
B (learning context)	0.050	1	0.050	0.054	0.828
Error B × P	3.700	4	0.925		
C (testing context)	0.450	1	0.450	0.286	0.621
Error C × P	6.300	4	1.575		
B × C	0.450	1	0.450	0.419	0.553
Error B × C × P	4.300	4	1.075		
P (participants)	6.500	4	1.633		

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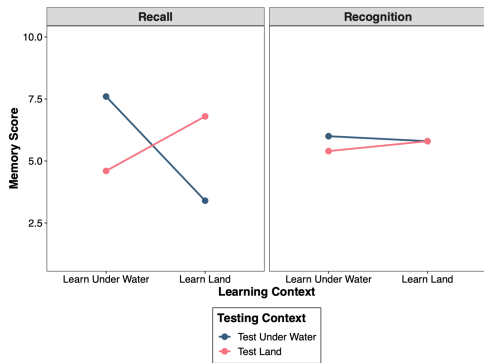
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## Interaction Plots For Memory and Context Study



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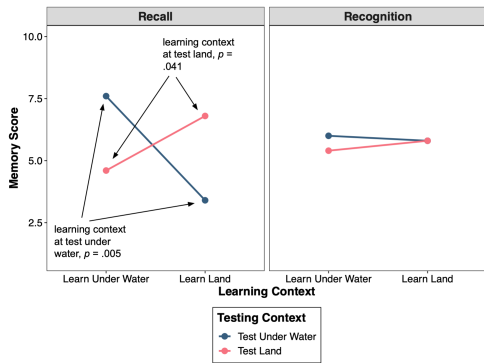
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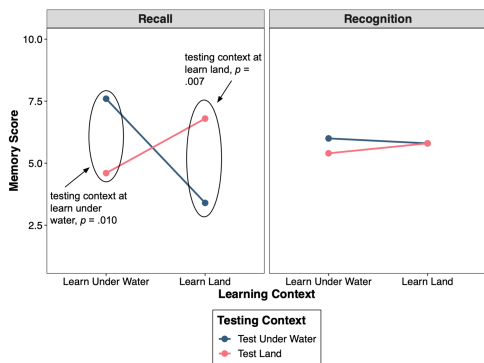
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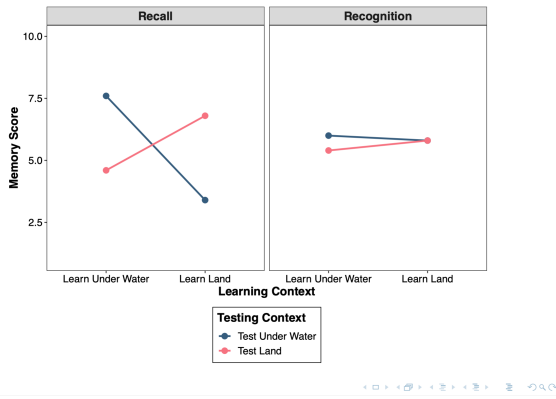
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## Learning To Pronounce Irregular Words: A 2 x 2 x 2 Mixed Design

- A researcher wants to investigate the development in children's ability to pronounce regular and irregular words
- The researcher adopts a 2 x 2 x 2 mixed design:
  - age (7 years old vs. 9 years old) is between-participants
  - word frequency (low vs. high) is within-participants
  - word type (regular vs. irregular) is within-participants
- Participants are given 10 words to pronounce in each category (40 words in total)
- Dependent measure is the number of pronunciation errors

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## Raw Data For Word Pronunciation Study

Table: A 2 x 2 x 2 factorial design

Factor A: Age	Level A <sub>1</sub> 7-years-old				Level A <sub>2</sub> 9-years-old				
	Level B <sub>1</sub> high		Level B <sub>2</sub> low		Level B <sub>1</sub> high		Level B <sub>2</sub> low		
Factor B: Frequency	Level B <sub>1</sub> high		Level B <sub>2</sub> low		Level B <sub>1</sub> high		Level B <sub>2</sub> low		
Factor C: Word type	C <sub>1</sub> reg	C <sub>2</sub> irr	C <sub>1</sub> reg	C <sub>2</sub> irr	C <sub>1</sub> reg	C <sub>2</sub> irr	C <sub>1</sub> reg	C <sub>2</sub> irr	
P <sub>1</sub>	6	7	5	6	P <sub>6</sub>	4	4	3	6
P <sub>2</sub>	7	5	6	7	P <sub>7</sub>	3	4	4	7
P <sub>3</sub>	5	6	7	6	P <sub>8</sub>	4	3	5	9
P <sub>4</sub>	6	7	5	7	P <sub>9</sub>	5	5	3	8
P <sub>5</sub>	6	6	5	7	P <sub>10</sub>	3	4	3	7

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## Aggregate Data For Word Pronunciation Study

Table: A 2 x 2 x 2 factorial design

	Level A <sub>1</sub> 7-years-old			Level A <sub>2</sub> 9-years-old			
	Level B <sub>1</sub> high	Level B <sub>2</sub> low	Overall	Level B <sub>1</sub> high	Level B <sub>2</sub> low	Overall	
Level C <sub>1</sub> regular	6.0	5.6	5.8	Level C <sub>1</sub> regular	3.8	3.6	3.7
Level C <sub>2</sub> irregular	6.2	6.6	6.4	Level C <sub>2</sub> irregular	4.0	7.4	5.7
Overall	6.1	6.1	6.1		3.9	5.5	4.7

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## ANOVA Table For Word Pronunciation Study

Source	Sum of Squares	Degrees of Freedom	Mean Square	F	P
A (age)	19.600	1	19.600	34.844	< .001
Between error S/A	4.500	8	0.562		
B (frequency)	6.400	1	6.400	5.885	0.042
Error B × S/A	8.700	8	1.087		
C (word type)	16.900	1	16.900	36.541	< .001
Error C × S/A	3.700	8	0.462		
A × B	6.400	1	6.400	5.885	0.042
Error B × S/A	8.700	8	1.087		
A × C	4.900	1	4.900	10.595	0.012
Error C × S/A	3.700	8	0.462		
B × C	12.100	1	12.100	17.600	0.003
Error B × C × S/A	5.500	8	0.688		
A × B × C	4.900	1	4.900	7.127	0.028
Error B × C × S/A	5.500	8	0.688		

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## Interpreting The Significant Three-Way Interaction

- To decompose our significant three-way interaction, we first need to decide which factor to split our design by
- The obvious choice is our between-participants factor A (age: 7 year olds vs. 9 year olds)
- Next, we perform two two-factor ANOVAs:
  - 2 (frequency: low vs. high) × 2 (word type: regular vs. irregular) ANOVA for the 7 year olds only
  - 2 (frequency: low vs. high) × 2 (word type: regular vs. irregular) ANOVA for the 9 year olds only

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## ANOVA Table For 7 Year Olds

Source	Sum of Squares	Degrees of Freedom	Mean Square	F	P
B (frequency)	0.000	1	0.000	0.000	1.000
Error B × P	2.500	4	0.625		
C (word type)	1.800	1	1.800	5.885	0.178
Error C × P	2.700	4	0.675		
B × C	0.800	1	0.800	5.885	0.405
Error B × C × P	3.700	4	0.925		
P (participants)	0.300	4	0.075		

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## ANOVA Table For 9 Year Olds

Source	Sum of Squares	Degrees of Freedom	Mean Square	F	P
B (frequency)	12.800	1	12.800	8.258	0.045
Error B × P	6.200	4	1.550		
C (word type)	20.000	1	20.000	80.000	< .001
Error C × P	1.000	4	0.250		
B × C	16.200	1	16.200	36.000	0.004
Error B × C × P	1.800	4	0.450		
P (participants)	4.200	4	1.050		

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## ANOVA Table For 9 Year Olds

Source	Sum of Squares	Degrees of Freedom	Mean Square	F	P
B (frequency)	12.800	1	12.800	8.258	0.045
Error B × P	6.200	4	1.550		
C (word type)	20.000	1	20.000	80.000	< .001
Error C × P	1.000	4	0.250		
B × C	16.200	1	16.200	36.000	0.004
Error B × C × P	1.800	4	0.450		
P (participants)	4.200	4	1.050		

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## Simple Main Effects Table For 9 Year Olds

Source	Sum of Squares	Degrees of Freedom	Mean Square	F	P
word frequency at					
regular words	0.100	1	0.100	0.065	0.812
irregular words	28.900	1	28.900	18.645	0.013
Error term	6.200	4	1.550		
word type at					
low frequency	36.100	1	36.100	144.400	< .001
high frequency	0.100	1	0.100	0.400	0.561
Error term	1.000	4	0.250		

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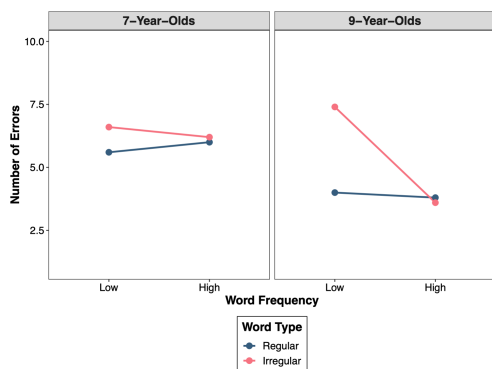
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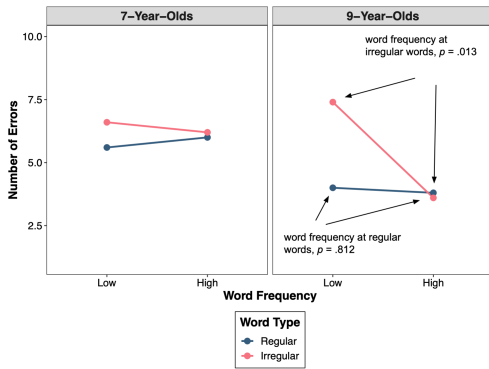
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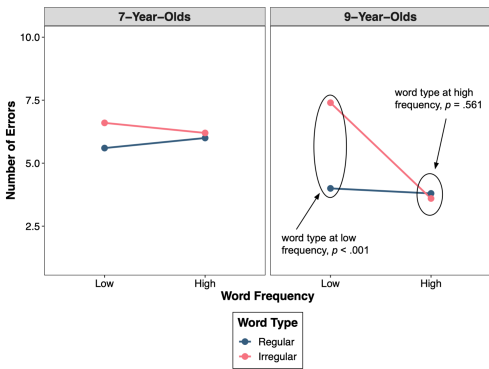
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## A Final Note On Interpreting Three-Way Interactions

- In both of these examples, one of the two-factor ANOVAs returned a significant interaction, whereas the other returned a non-significant interaction
- This will **not** always be the case
- Sometimes the interaction for each two-factor ANOVA will be significant and both will need to be followed up with a simple main effects analysis
- Under these conditions, the simple main effects for the two interactions will differ in direction and/or size of their trends

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## General Points

- As always, start at the bottom of the ANOVA table and work your way up
- If the three-way interaction is significant, then this must be analysed
- If not, then each of the significant two-way interactions should be analysed independently
- If none of the two-way interactions is significant, the ANOVA results may be described in terms of the main effects, with follow-up tests for any factors with three or more levels

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## In Next Week's Lab ...

- Running a three-factor (fully within-participants and mixed) ANOVA in R

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## References

Roberts, M. J., & Russo, R. (1999, Chapter 12). *A student's guide to Analysis of Variance*. Routledge: London.

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